# **NeuroImaging Data Processing**

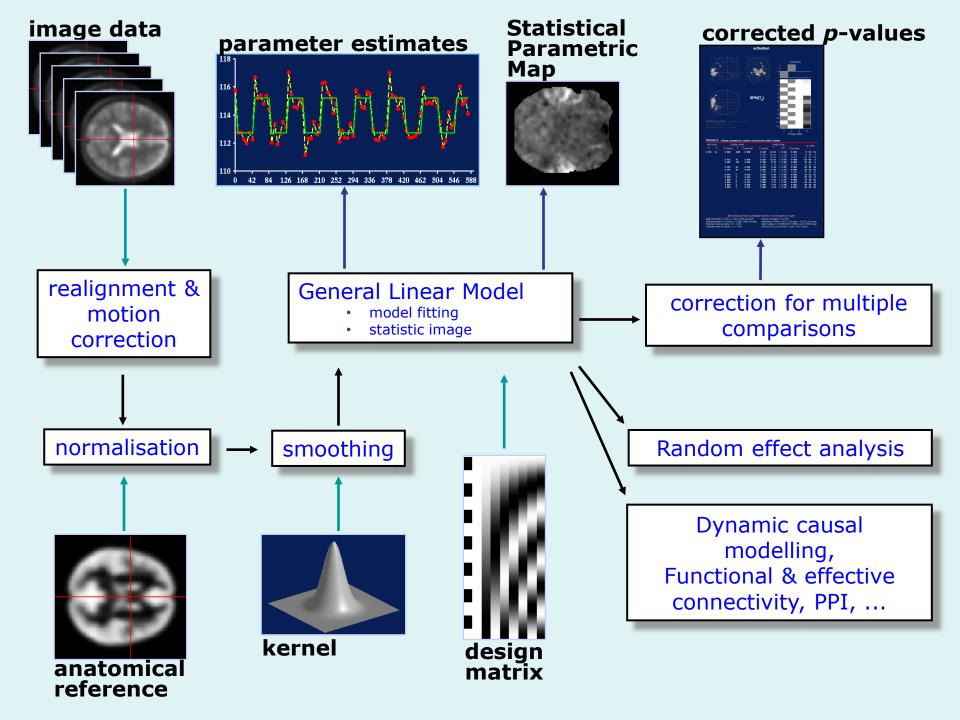
aka. Statistical Parametric Mapping short course

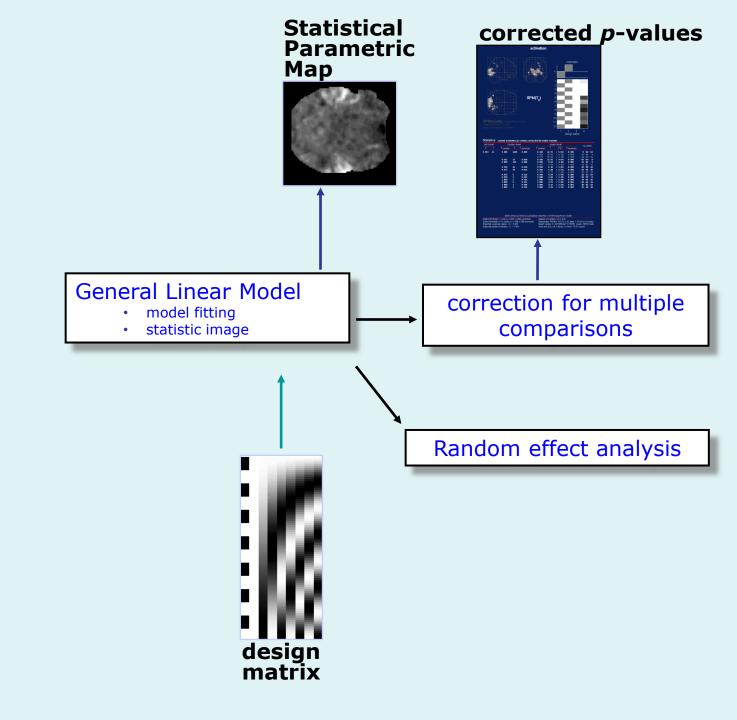
## Course 4:

Multiple comparison problem & levels of inference









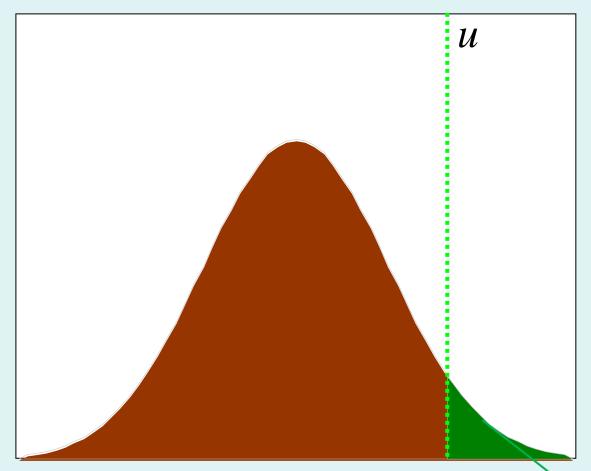
## Content

- Introduction
- Family-wise error rate (FWER)
- False discovery rate (FDR)
- Levels of inference in SPM
- Non-parametric permutation test
- Conclusion

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- Introduction
  - Single voxel inference
  - Multiple comparison problem
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# Single voxel inference



Null distribution of test statistic T

Null Hypothesis H<sub>0</sub>: zero activation

Decision rule (threshold) u: determines false positive rate  $\alpha$ 

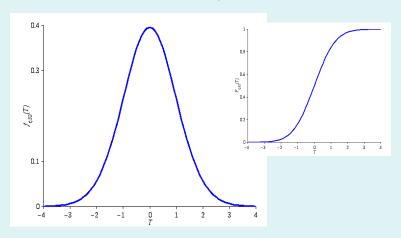
 $\Rightarrow$  Choose u to give acceptable  $\alpha$  under  $H_0$ 

$$\alpha = p(t > u|H_0)$$

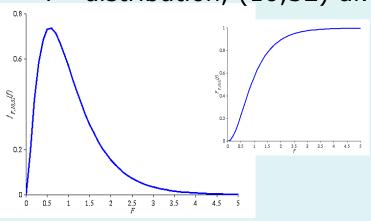
# Classical hypothesis testing...

- Null hypothesis H
  - test statistic
  - null distributions
- Hypothesis test
  - control Type I error
    - incorrectly reject H
  - test level α
    - Pr("reject"  $H \mid H$ )  $\leq \alpha$
- p -value
  - min  $\alpha$  at which H rejected
  - $Pr(T \ge t \mid H)$
  - characterising "surprise"

*t* –distribution, 32 df.



F –distribution, (10,32) df.



# Sensitivity & specificity

**TRUTH** 

#### **ACTION**

	Don't reject	Reject
H <sub>0</sub> true	True Negative	False Positive
H <sub>0</sub> false	False Negative	True Positive

```
Sensitivity = TP/(TP+FN) = \beta

Specificity = TN/(TN+FP) = 1 - \alpha

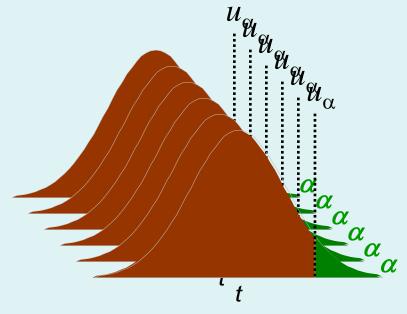
FP = Type I error or 'error'

FN = Type II error

\alpha = p-value/FP rate/error rate/significance level

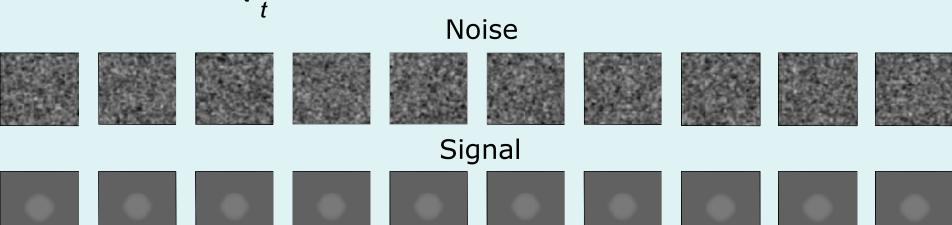
\beta = power
```

# Multiple tests

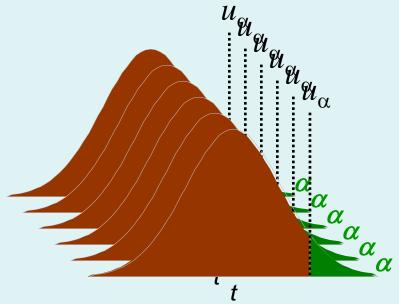


If we have 100000 voxels,  $\alpha$ =0.05  $\Rightarrow$  **5000 false positive voxels**.

This is clearly undesirable! Need to define a *null hypothesis* for a *collection of tests*.



# Multiple tests



If we have 100000 voxels,  $\alpha$ =0.05  $\Rightarrow$  **5000 false positive voxels**.

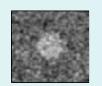
This is clearly undesirable! Need to define a *null hypothesis* for a *collection of tests*.

#### Noisy data



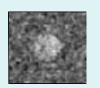


















Use of 'uncorrected' p-value,  $\alpha = 0.1$ 





















11.3% 11.3% 12.5

12.5% 10.8%

8% 11.5%

10.0%

10.7%

11.2%

10.2%

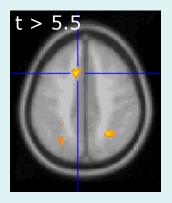
9.5% 10

Percentage of Null Pixels that are False Positives

# Assessing statistics images

# Where's the signal?

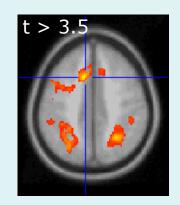
High Threshold



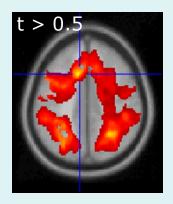
**Good Specificity** 

Poor Power (risk of false negatives)

Med. Threshold



Low Threshold



Poor Specificity (risk of false positives)

**Good Power** 

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- Introduction
- Family-wise error rate (FWER)
  - Family-wise Null hypothesis
  - Bonferroni correction
  - Random Field Theory
- False discovery rate (FDR)
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# Family-Wise Null Hypothesis

#### Family-Wise Null Hypothesis:

Activation is zero everywhere

If we reject a voxel null hypothesis at any voxel, we reject the family-wise Null hypothesis

A FP **anywhere** in the image gives a **Family Wise Error** (FWE)

Family-Wise Error rate (FWER) = 'corrected' p-value























Use of 'corrected' p-value,  $\alpha = 0.1$ 





















## Bonferroni correction

The Family-Wise Error rate (FWER),  $\alpha_{FWE}$ , for a family of N tests follows the inequality:

$$\alpha_{FWE} \leq N\alpha$$

where  $\alpha$  is the test-wise error rate.

Therefore, to ensure a particular FWER choose:

$$\alpha = \frac{\alpha_{FWE}}{N}$$

This correction does not require the tests to be independent but becomes very stringent if dependence.

# Bonferroni correction, example

- Experiment with N = 100000 independent voxels and 40 d.f.
  - v = unknown corrected probability threshold,
  - find v such that family-wise error rate  $\alpha = 0.05$

#### Bonferroni correction:

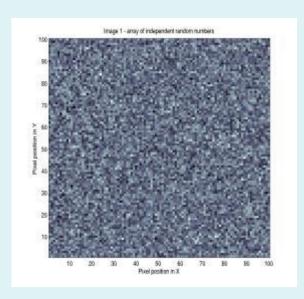
- probability that all tests are below the threshold,
- use  $v = \alpha / N$
- here v=0.05/100000=0.0000005
  - $\Rightarrow$  threshold t = 5.77

#### Interpretation:

Bonferroni procedure gives a corrected p-value,

- i.e. for a t statistics = 5.77,
- uncorrectd p value = 0.0000005
- corrected p value = 0.05

## Bonferroni & independent observations

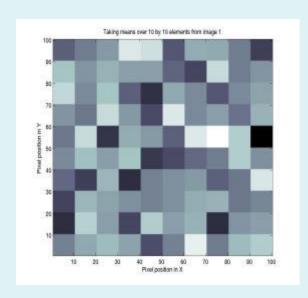


#### 100 by 100 voxels.

**10000** independent measures Fix the  $P^{FWE} = 0.05$ , z threshold?

#### Bonferroni:

v = 0.05 / 10000 = 0.000005 $\Rightarrow$  threshold z = 4.42



#### 100 by 100 voxels.

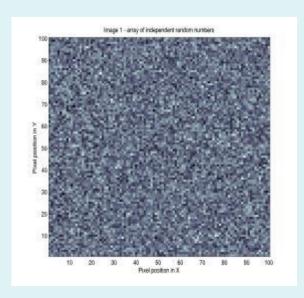
**100** independent measures Fix the  $P^{FWE} = 0.05$ , z threshold?

#### Bonferroni:

v = 0.05 / 100 = 0.0005 $\Rightarrow$  threshold z = 3.29

 $v = \alpha/n_i$  where  $n_i$  is the number of independent observations.

## Bonferroni & independent observations

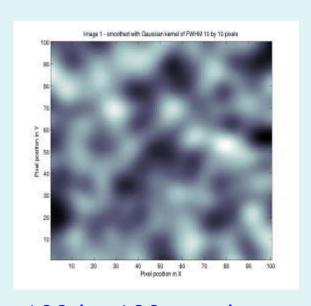


100 by 100 voxels.

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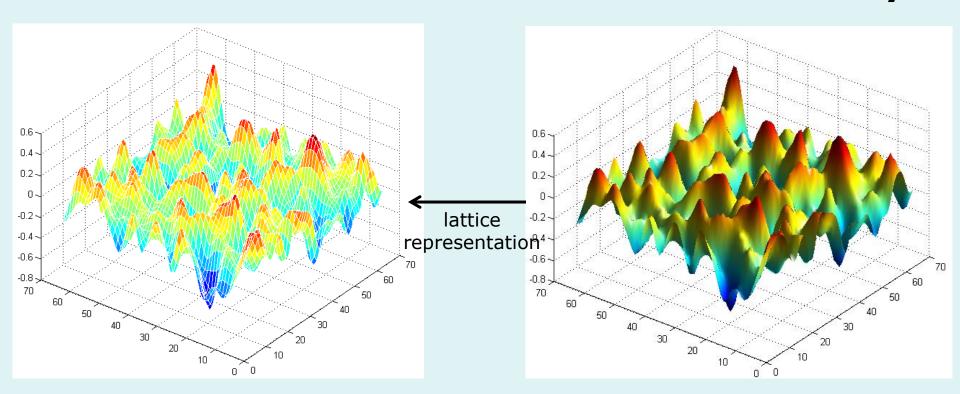


100 by 100 voxels.

How many independent measures ???

# Random Field Theory

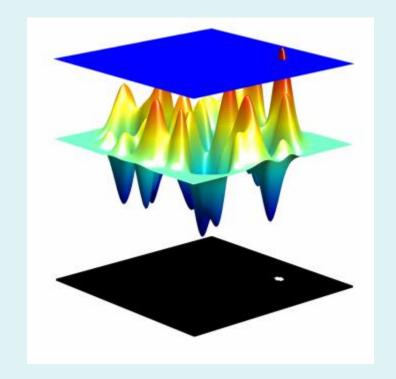
- ⇒ Consider a statistic image as a discretisation of a continuous underlying random field.
- ⇒ Use results from continuous random field theory.



## RFT and Euler Characteristic

#### **Euler Characteristic** $\chi_{u}$ :

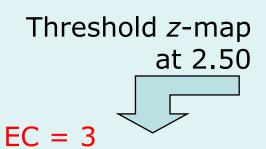
- Topological measure  $\chi_u = \#$  blobs # holes
- at high threshold u:  $\chi_u = \#$  blobs

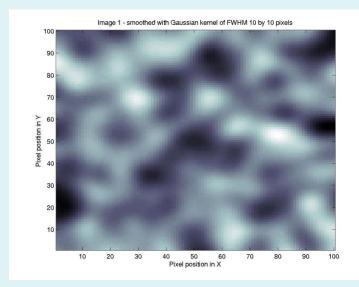


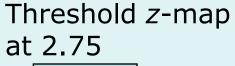
$$FWER = p(FWE)$$

$$\approx E[\chi_u]$$

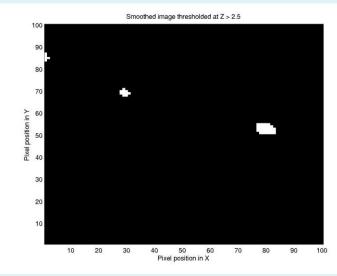
## Euler characteristic...

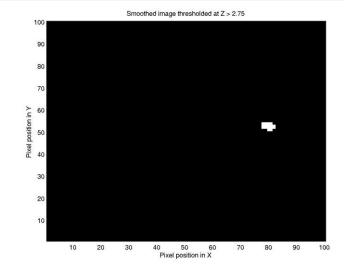






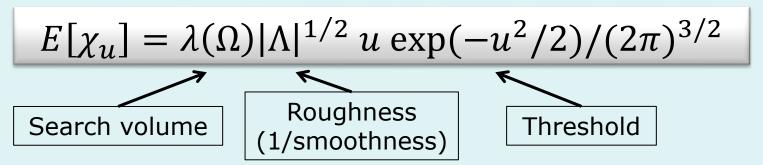






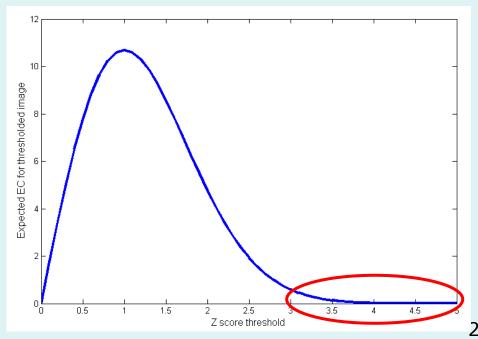
# Expected Euler Characteristic

2D Gaussian Random Field



100 x 100 Gaussian Random Field with FWHM=10 smoothing

$$\alpha_{FWE} = 0.05 \Rightarrow u_{RFT} = 3.8$$
 $(u_{BONF} = 4.42, u_{uncorr} = 1.64)$ 



## **Smoothness**

#### **Smoothness parameterised in terms of FWHM:**

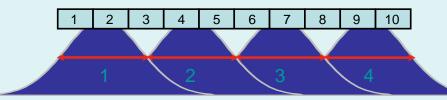
Size of Gaussian kernel required to smooth i.i.d. noise to have same smoothness as observed null (standardized) data.



#### **RESELS (Resolution Elements):**

1 RESEL =  $FWHM_xFWHM_yFWHM_z$ 

RESEL Count R = volume of search region in units of smoothness

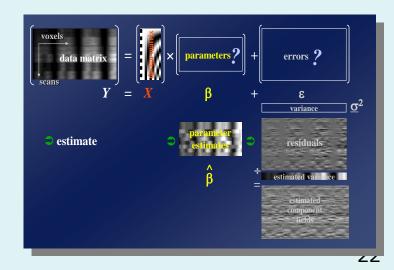


Eg: 10 voxels, 2.5 FWHM, 4 RESELS

The number of resels is similar, but not identical to the number independent observations.

### Smoothness estimated from spatial derivatives of standardised residuals:

Yields an RPV image containing local roughness estimation.



## RFT intuition

## Corrected *p*-value for statistic value *t*

$$p_c = p(\max T > t)$$

$$\approx E[\chi_t]$$

$$\propto \lambda(\Omega) |\Lambda|^{1/2} t \exp(-t^2/2)$$

- Statistic value t increases ?
  - $-p_c$  decreases (better signal)
- Search volume increases  $(\lambda(\Omega) \uparrow)$ ?
  - $-p_c$  increases (more severe correction)
- Smoothness increases  $(|\Lambda|^{1/2}\downarrow)$ ?
  - $-p_c$  decreases (less severe correction)

# RFT, unified theory

## General form for expected Euler characteristic

t, F &  $\chi^2$  fields • restricted search regions • D dimensions

$$E[\chi_u(\Omega)] = \sum_{d=0}^{D} R_d(\Omega) \rho_d(u)$$

 $R_d(\Omega)$ : d-dimensional Lipschitz-Killing curvatures of  $\Omega$  ( $\approx$  intrinsic volumes):

-function of dimension, space  $\Omega$  and smoothness:

 $R_0(\Omega) = \chi(\Omega)$  Euler characteristic of  $\Omega$ 

 $R_1(\Omega)$  = resel diameter

 $R_2(\Omega)$  = resel surface area

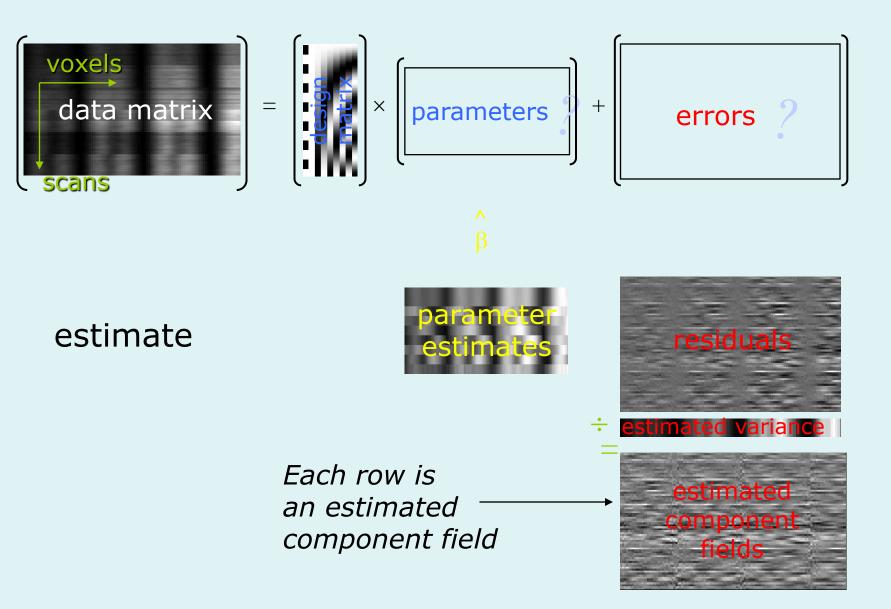
 $R_3(\Omega)$  = resel volume

 $\rho_d(\mathbf{u})$ : d-dimensional EC density of the field

- function of dimension and threshold, specific for RF type:

E.g. Gaussian RF:

# Estimated component fields

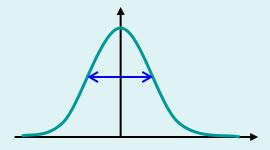


# Smoothness, PRF, ResEls...

- Smoothness √|Λ|
  - variance-covariance matrix of partial derivatives (possibly location dependent)

$$\Lambda = \begin{pmatrix} \operatorname{var} \left[ \frac{\partial e}{\partial x} \right] & \operatorname{cov} \left[ \frac{\partial e}{\partial x}, \frac{\partial e}{\partial y} \right] & \operatorname{cov} \left[ \frac{\partial e}{\partial x}, \frac{\partial e}{\partial z} \right] \\ \operatorname{cov} \left[ \frac{\partial e}{\partial x}, \frac{\partial e}{\partial y} \right] & \operatorname{var} \left[ \frac{\partial e}{\partial y} \right] & \operatorname{cov} \left[ \frac{\partial e}{\partial y}, \frac{\partial e}{\partial z} \right] \\ \operatorname{cov} \left[ \frac{\partial e}{\partial x}, \frac{\partial e}{\partial z} \right] & \operatorname{cov} \left[ \frac{\partial e}{\partial y}, \frac{\partial e}{\partial z} \right] & \operatorname{var} \left[ \frac{\partial e}{\partial z} \right] \end{pmatrix}$$

Point Response Function PRF



 Full Width at Half Maximum FWHM. Approximate the peak of the Covariance function with a Gaussian

- Gaussian PRF
  - Σ kernel var/cov matrix
  - ACF  $2\Sigma$
  - $\Lambda = (2\Sigma)^{-1}$

 $\Rightarrow$ FWHM f =  $\sigma \sqrt{8\ln(2)}$ 

$$\Rightarrow \text{FWHM } f = \sigma \sqrt{8 \ln(2)}$$

$$- \Sigma = \begin{bmatrix} f_x & 0 & 0 \\ 0 & f_y & 0 \\ 0 & 0 & f_z \end{bmatrix} \frac{1}{8 \ln(2)}$$

$$ightherefore the constant  $f(x) = \frac{1}{2} \ln(2)$$$

for high thresholds u

 $\Rightarrow \sqrt{|\Lambda|} = (4\ln(2))^{3/2} / (f_x \times f_y \times f_z)$ 

- Resolution Element (ResEI)
  - Resel dimensions  $(f_x \times f_y \times f_z)$
  - $-R_3(\Omega) = \lambda(\Omega) / (f_x \times f_y \times f_z)$ if strictly stationary

$$E[\chi(A_u)] = R_3(\Omega) (4\ln(2))^{3/2} (u^2 - 1) \exp(-u^2/2)$$

$$\approx R_3(\Omega) (1 - \Phi(u))$$

# RFT assumptions

- The statistic image is assumed to be a good lattice representation of an underlying random field with a multivariate Gaussian distribution.
- These fields are continuous, with an autocorrelation function twice differentiable at the origin.
- ➤ The threshold chosen to define clusters is high enough such that the expected EC is a good approximation to the number of clusters.
- > The lattice approximation is reasonable, which implies the smoothness is relatively large compared to the voxel size.
- ➤ The errors of the specified statistical model are normally distributed, which implies the model is not misspecified.
- Smoothness of the data is unknown and estimated: very precise estimate by pooling over voxels ⇒ stationarity assumption.

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## FDR illustration:

# Noise Signal Signal+Noise

#### Control of Per Comparison Rate at 10%





















11.3% 11.3% 12.5% 10.8% 11.5% 10.0% 10.7% 11.2% 10.2% 9.5% Percentage of Null Pixels that are False Positives

#### Control of Familywise Error Rate at 10%



















**FWF** 



Occurrence of Familywise Error

#### Control of False Discovery Rate at 10%





















6.7% 10.4% 14.9% 9.3% 16.2% 13.8% 14.0% 10.5% 12.2% 8.7% Percentage of Activated Pixels that are False Positives

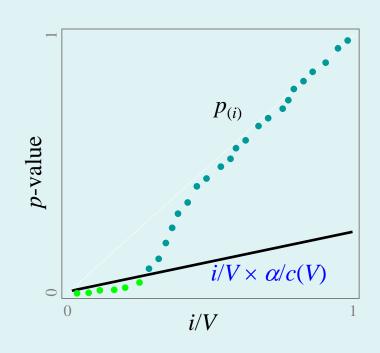
## Benjamini & Hochberg Procedure

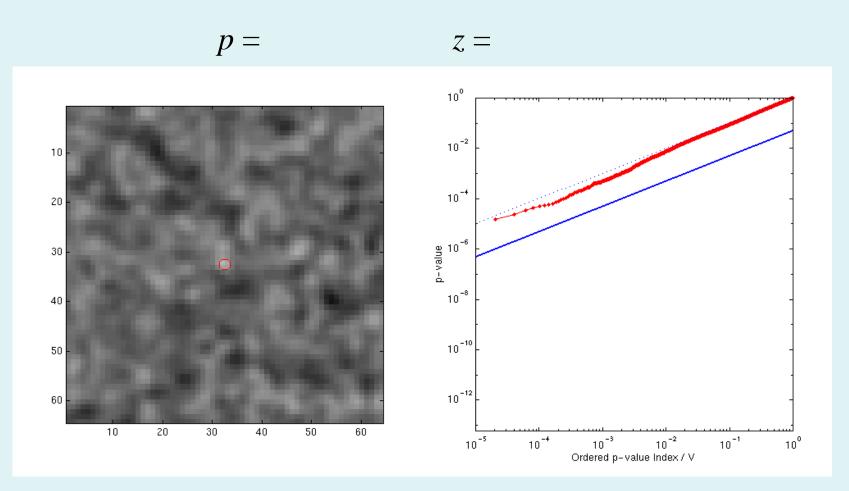
- Select desired limit  $\alpha$  on E(FDR)
- Order p-values,  $p_{(1)} \le p_{(2)} \le ... \le p_{(V)}$
- Let r be largest i such that

$$p_{(i)} \leq i/V * \alpha$$

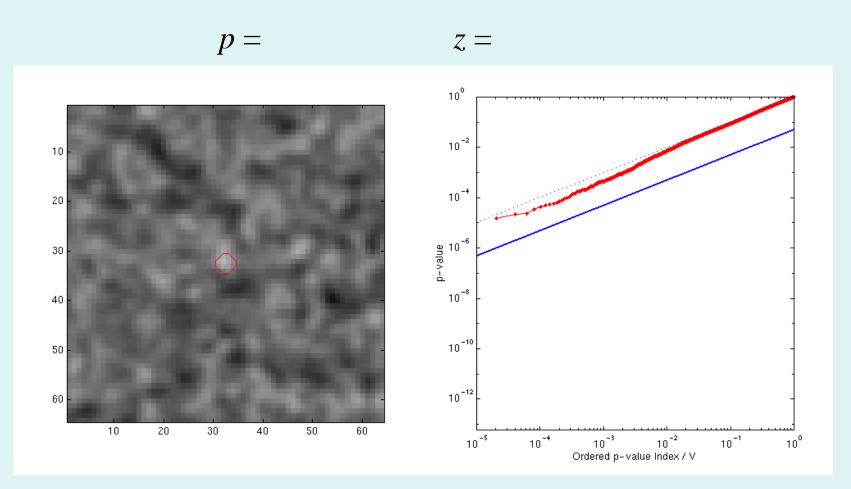
 Reject all hypotheses corresponding to

$$p_{(1)}, \ldots, p_{(r)}$$

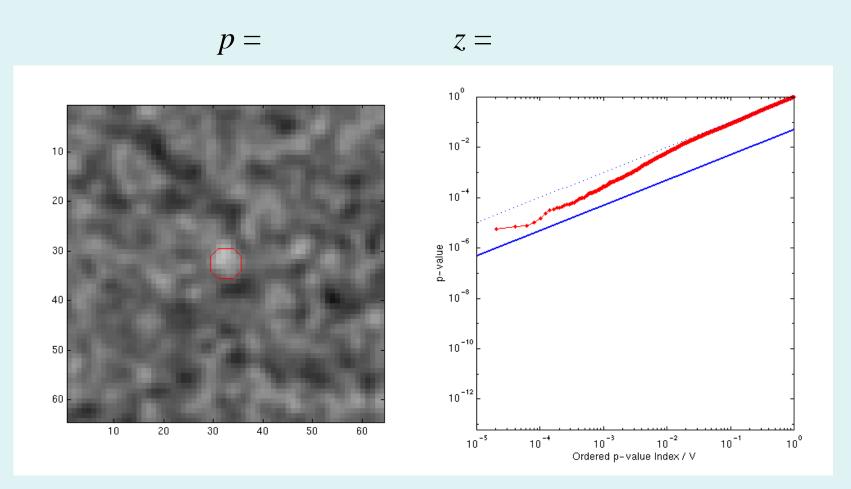




Signal Intensity 3.0 Signal Extent 1.0 Noise Smoothness 3.0



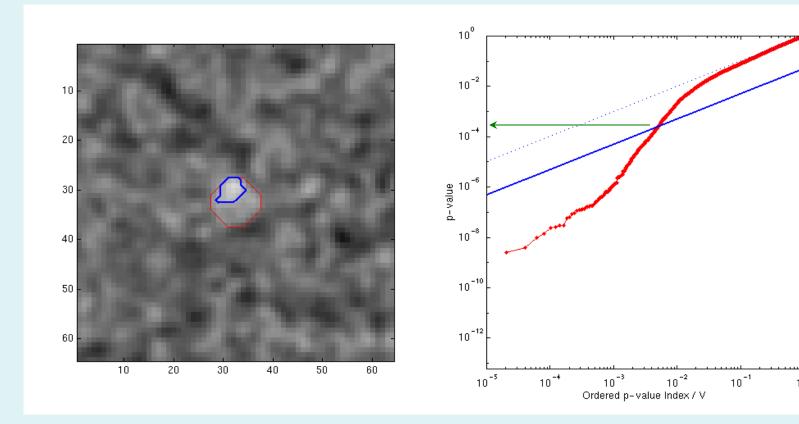
Signal Intensity 3.0 Signal Extent 2.0 Noise Smoothness 3.0



Signal Intensity 3.0 Signal Extent 3.0 Noise Smoothness 3.0

$$p = 0.000252$$
  $z = 3.48$ 

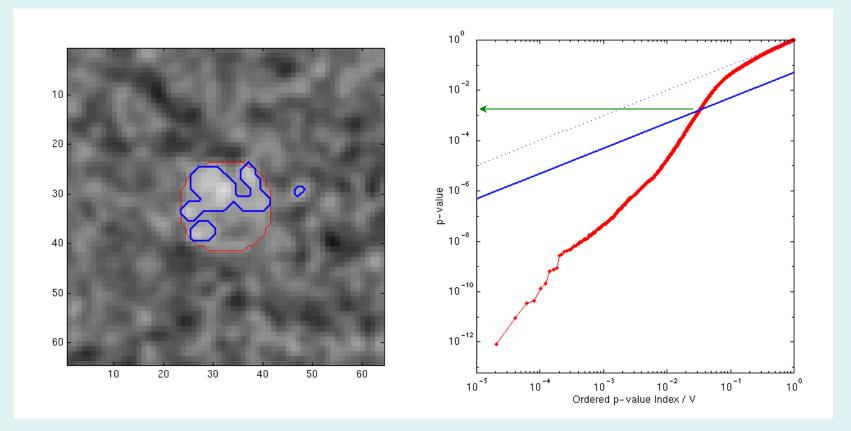
$$z = 3.48$$



Signal Intensity 3.0 Signal Extent 5.0 Noise Smoothness 3.0

$$p = 0.001628$$
  $z = 2.94$ 

$$z = 2.94$$

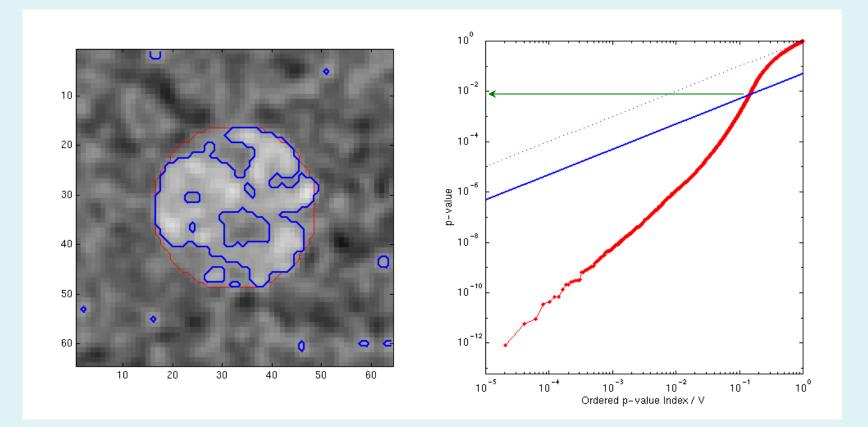


Signal Intensity 3.0 Signal Extent 9.5 Noise Smoothness 3.0

# **B&H: Varying Signal Extent**

$$p = 0.007157$$
  $z = 2.45$ 

$$z = 2.45$$

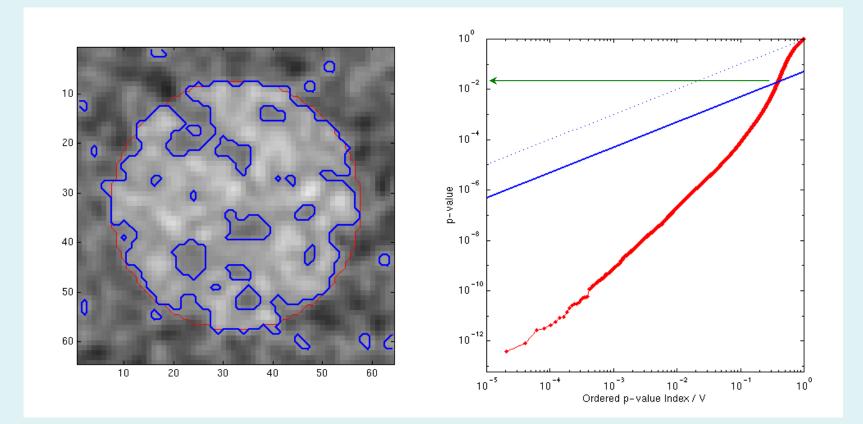


Signal Extent16.5 Noise Smoothness 3.0 Signal Intensity 3.0

# **B&H: Varying Signal Extent**

$$p = 0.019274$$
  $z = 2.07$ 

$$z = 2.07$$



Signal Intensity 3.0 Noise Smoothness 3.0 Signal Extent 25.0

# Benjamini & Hochberg: Properties

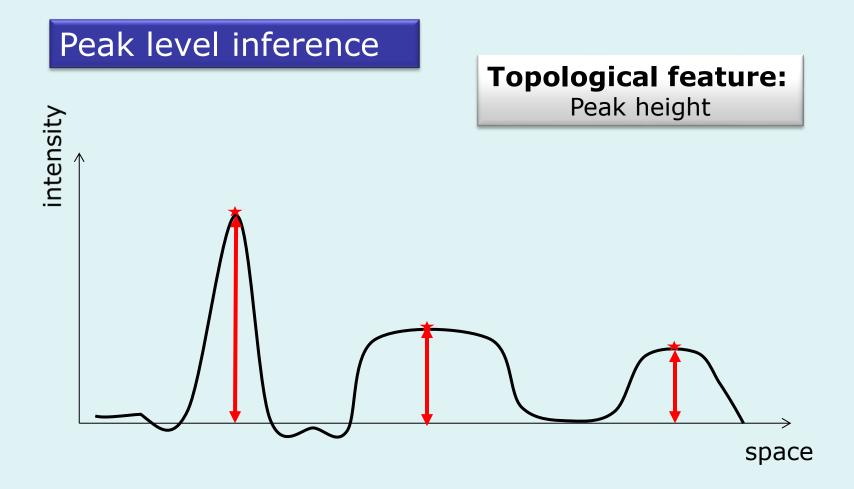
#### Adaptive

- Larger the signal, the lower the threshold
- Larger the signal, the more false positives
  - False positives constant as fraction of rejected tests
  - Not a problem with imaging's sparse signals
- Smoothness OK
  - Smoothing introduces positive correlations

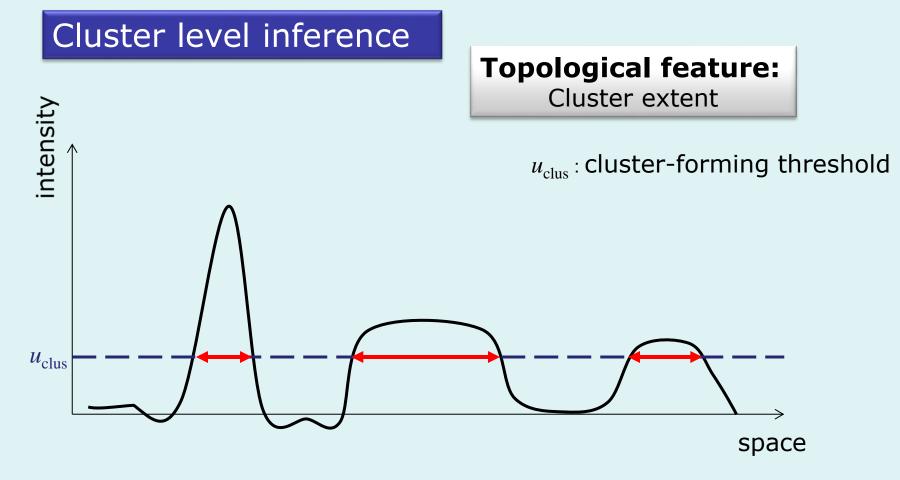
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  - Topological inference
  - Small volume correction
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# Topological inference



# Topological inference



You MUST use a sufficiently high clusterforming threshold  $u_{clus}$ , i.e.  $p_{unc} < .001$ 

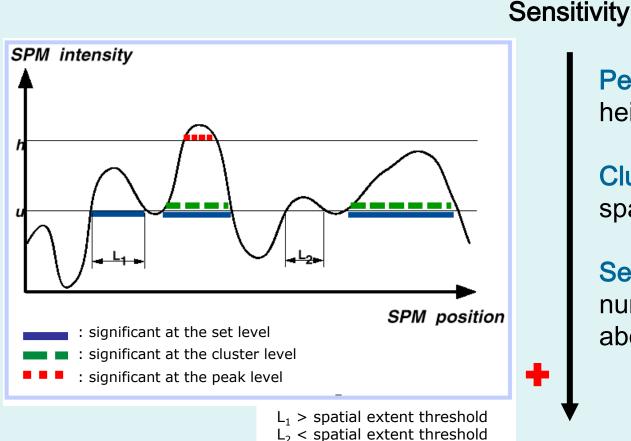
# Topological inference

#### Set level inference

# Number of clusters intensity $u_{\rm clus}$ : cluster-forming threshold $u_{\rm clus}$ space

**Topological feature:** 

# Peak, cluster & set level inference



Peak level test: height of local maxima

Cluster level test: spatial extent above u

Set level test: number of clusters above u

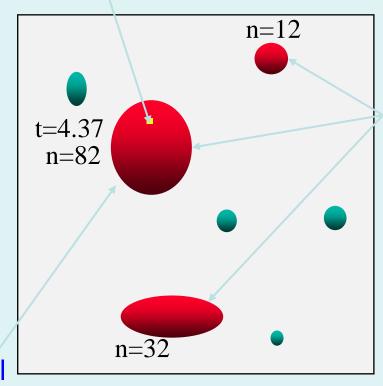
Regional

specificity

#### Levels of inference...

#### Voxel-level

$$P(c \ge 1 \mid n \ge 0, t \ge 4.37) = 0.048$$
 (corrected)  
 $P(t \ge 4.37) = 1 - \Phi\{4.37\} < 0.001$  (uncorrected)



#### Cluster-level

 $P(c \ge 1 \mid n \ge 82, t \ge 3.09) = 0.029$  (corrected)  $P(n \ge 82 \mid t \ge 3.09) = 0.019$  (uncorrected)

#### **Omnibus**

 $P(c \ge 7 \mid n \ge 0, t \ge 3.09) = 0.031$ 

#### Set-level

 $P(c \ge 3 \mid n \ge 12, t \ge 3.09) = 0.019$ 

#### **Parameters**

u - 3.09

k - 12 voxels

S  $-32^3$  voxels

FWHM - 4.7 voxels

D - 3

#### Small volume correction

If one has some *a priori* idea of where an activation should be, one can pre-specify a small search space and make the appropriate correction instead of having to control for the entire search space

- mask defined by (probabilistic) anatomical atlases
- mask defined by separate "functional localisers"
- mask defined by orthogonal contrasts
- search volume around previously reported coordinates

With no prior hypothesis:

- 1. Test whole volume.
- 2. Identify SPM peak.
- 3. Then make a test assuming a single voxel.

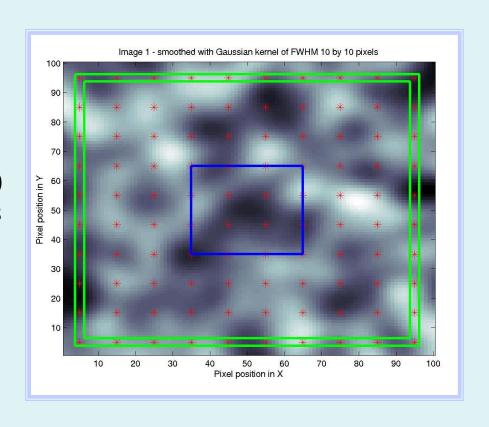
#### **Small Volume Correction**

SVC = correction for multiple comparison in a user's defined volume 'of interest'.

Shape and size of volume become important for small or oddly shaped volume!

Example of SVC (900 voxels)

- compact volume: samples from maximum 16 resels
- spread volume: sample from up to 36 resels
  - ⇒ threshold higher for spread volume than compact volume.



# Small volume correction, topology

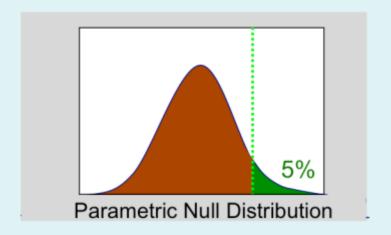
Table 3. Representative examples of resel counts and critical values,								
	Vol.		Resel	counts		t for	$P(M \ge$	≥ t) =
Search region $V$	(cc)	$R_0(V)$	$R_1(V)$	$R_2(V)$	$R_3(V)$	0.10	0.05	0.01
Single voxel	0	1	0	0	0	1.28	1.64	2.33
Head Of Caudate	7	0	6.18	4.63	0.65	2.75	3.02	3.55
Putamen	12	1	7.32	6.80	1.18	2.89	3.15	3.66
Globus Pallidus	3	0	4.03	2.29	0.24	2.49	2.78	3.35
Thalamus	11	1	4.94	5.14	1.13	2.79	3.05	3.59
Anterior Cingulate Gyrus	9	1	8.20	5.79	0.86	2.86	3.11	3.63
Posterior Cingulate Gyrus	6	1	5.32	3.85	0.58	2.70	2.97	3.51
Cingulate Gyri	15	0	12.89	9.63	1.44	3.03	3.27	3.77
Superior Frontal Gyrus	80	1	15.64	25.69	8.97	3.38	3.60	4.07
Middle Frontal Gyrus	57	1	14.89	21.14	6.23	3.31	3.53	4.00
Inferior Frontal Gyrus	37	1	11.22	14.25	4.06	3.17	3.41	3.89
Precentral Gyrus	32	1	12.30	14.23	3.40	3.16	3.40	3.88
Frontal Gyri	207	1	19.30	53.39	23.63	3.63	3.84	4.28
Occipital Lobe	65	-1	10.68	23.11	7.17	3.32	3.55	4.02
4mm shell	254	2	0.54	207.27	15.88	3.85	4.04	4.45
Whole brain	1294	1	20.43	107.09	153.42	4.05	4.23	4.63

#### Content

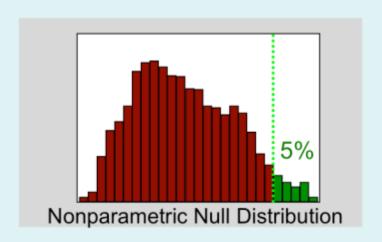
- Introduction
- Family-wise error rate (FWER)
- False discovery rate (FDR)
- Levels of inference in SPM
- Non-parametric permutation test
- Conclusion

# Non-parametric permutation test

- Parametric methods
  - Assume distribution of statistic under null hypothesis



- Nonparametric methods
  - Use data to find distribution of statistic under null hypothesis
  - Any statistic!



Data from V1 voxel in visual stim. experiment
 A: Active, flashing checkerboard
 B: Baseline, fixation
 blocks, ABABAB
 Just consider block averages...



- Null hypothesis H<sub>o</sub>
  - No experimental effect, A & B labels arbitrary
- Statistic
  - Mean difference

- Under H<sub>o</sub>
  - Consider all equivalent relabelings

AAABBB	ABABAB	BAAABB	BABBAA
AABABB	ABABBA	BAABAB	BBAAAB
AABBAB	ABBAAB	BAABBA	BBAABA
AABBBA	ABBABA	BABAAB	BBABAA
ABAABB	ABBBAA	BABABA	BBBAAA

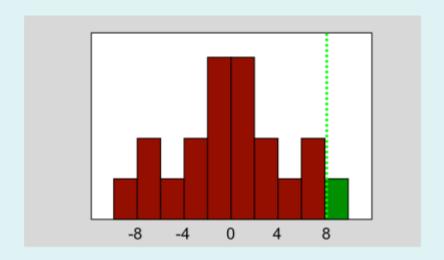
- Under H<sub>o</sub>
  - Consider all equivalent relabelings
  - Compute all possible statistic values

AAABBB 4.82	ABABAB 9.45	BAAABB -1.48	BABBAA -6.86
AABABB -3.25	ABABBA 6.97	BAABAB 1.10	BBAAAB 3.15
AABBAB -0.67	ABBAAB 1.38	BAABBA -1.38	BBAABA 0.67
AABBBA -3.15	ABBABA -1.10	<b>BABAAB -6.97</b>	BBABAA 3.25
ABAABB 6.86	ABBBAA 1.48	<b>BABABA -9.45</b>	<b>BBBAAA -4.82</b>

- Under H<sub>o</sub>
  - Consider all equivalent relabelings
  - Compute all possible statistic values
  - Find 95%ile of permutation distribution

AAABBB 4.82	ABABAB 9.45	BAAABB -1.48	BABBAA -6.86
AABABB -3.25	ABABBA 6.97	BAABAB 1.10	BBAAAB 3.15
AABBAB -0.67	ABBAAB 1.38	BAABBA -1.38	BBAABA 0.67
AABBBA -3.15	ABBABA -1.10	<b>BABAAB -6.97</b>	BBABAA 3.25
ABAABB 6.86	ABBBAA 1.48	<b>BABABA -9.45</b>	<b>BBBAAA -4.82</b>

- Under H<sub>o</sub>
  - Consider all equivalent relabelings
  - Compute all possible statistic values
  - Find 95%ile of permutation distribution

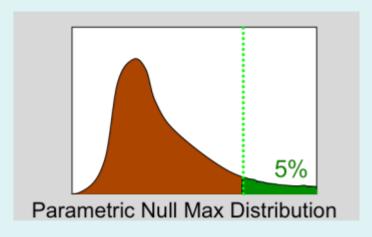


- Under H<sub>o</sub>
  - Consider all equivalent relabelings
  - Compute all possible statistic values
  - Find 95%ile of permutation distribution

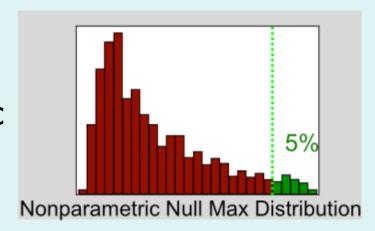
AAABBB 4.82	ABABAB 9.45	BAAABB -1.48	BABBAA -6.86
AABABB -3.25	ABABBA 6.97	BAABAB 1.10	BBAAAB 3.15
AABBAB -0.67	ABBAAB 1.38	BAABBA -1.38	BBAABA 0.67
AABBBA -3.15	ABBABA -1.10	<b>BABAAB -6.97</b>	BBABAA 3.25
ABAABB 6.86	ABBBAA 1.48	<b>BABABA -9.45</b>	<b>BBBAAA -4.82</b>

#### Controlling FWER: Permutation Test

- Parametric methods
  - Assume distribution of max statistic under null hypothesis



- Nonparametric methods
  - Use data to find distribution of max statistic under null hypothesis
  - Again, any max statistic!



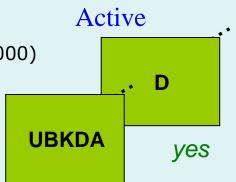
#### Permutation Test & Exchangeability

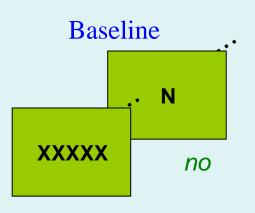
- Exchangeability is fundamental
  - Def: Distribution of the data unperturbed by permutation
  - Under H<sub>0</sub>, exchangeability justifies permuting data
  - Allows us to build permutation distribution
- Subjects are exchangeable
  - Under H<sub>o</sub>, each subject's A/B labels can be flipped
- Are fMRI scans exchangeable under H<sub>o</sub>?
  - If no signal, can we permute over time?

### Permutation Test & Exchangeability

- fMRI scans are *not* exchangeable
  - Permuting disrupts order, temporal autocorrelation
- *Intra*subject fMRI permutation test
  - Must decorrelate data, model before permuting
  - What is correlation structure?
    - Usually must use parametric model of correlation
  - E.g. Use wavelets to decorrelate
    - Bullmore et al 2001, HBM 12:61-78
- Intersubject fMRI permutation test
  - Create difference image for each subject
  - For each permutation, flip sign of some subjects

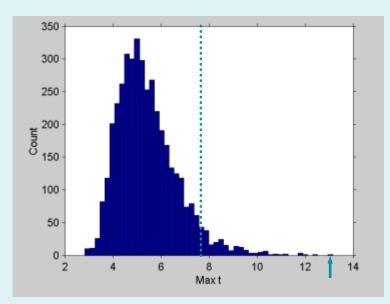
- fMRI Study of Working Memory
  - 12 subjects, block design Marshuetz et al (2000)
  - Item Recognition
    - Active: View five letters, 2s pause, view probe letter, respond
    - Baseline: View XXXXX, 2s pause, view Y or N, respond
- Second Level RFX
  - Difference image, A-B constructed for each subject
  - One sample, smoothed variance t test



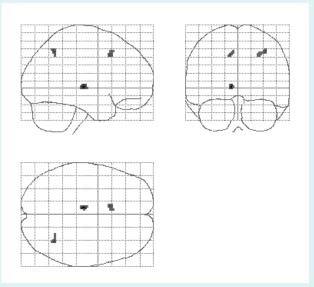


#### Permute!

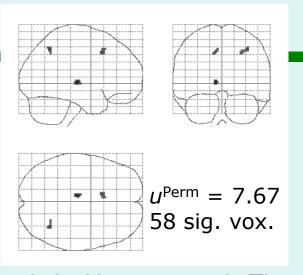
- $-2^{12} = 4,096$  ways to flip 12 A/B labels
- For each, note maximum of t image



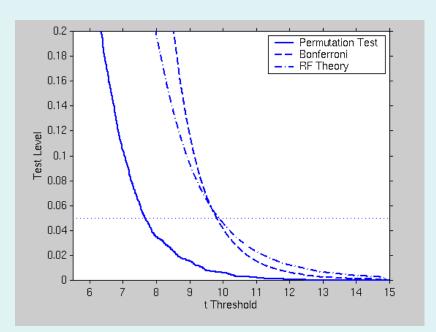
Permutation Distribution Maximum *t* 



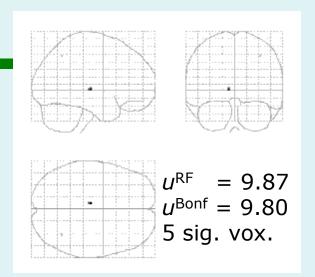
Maximum Intensity Projection
Thresholded *t* 



 $t_{11}$  Statistic, Nonparametric Threshold



Test Level vs.  $t_{11}$  Threshold



 $t_{11}$  Statistic, RF & Bonf. Threshold

- Compare with Bonferroni  $\alpha = 0.05/110,776$
- Compare with parametric RFT 110,776 2×2×2mm voxels 5.1×5.8×6.9mm FWHM

smoothness 462.9 RESELs

# Generalization: RFT vs Bonf. vs Perm.

		t Threshold (0.05 Corrected)		
	df	RF	Bonf	Perm
Verbal Fluency	4	4701.32	42.59	10.14
Location Switching	9	11.17	9.07	5.83
Task Switching	9	10.79	10.35	5.10
Faces: Main Effect	11	10.43	9.07	7.92
Faces: Interaction	11	10.70	9.07	8.26
Item Recognition	11	9.87	9.80	7.67
Visual Motion	11	11.07	8.92	8.40
Emotional Pictures	12	8.48	8.41	7.15
Pain: Warning	22	5.93	6.05	4.99
Pain: Anticipation	22	5.87	6.05	5.05

# RFT vs Bonf. vs Perm.

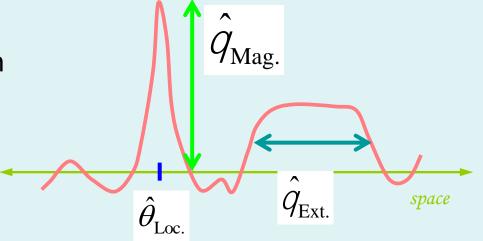
		No. Significant Voxels (0.05 Corrected)  t			
	df	RF	Bonf	Perm	
Verbal Fluency	4	0	0	0	
Location Switching	9	0	0	158	
Task Switching	9	4	6	2241	
Faces: Main Effect	11	127	371	917	
Faces: Interaction	11	0	0	0	
Item Recognition	11	5	5	58	
Visual Motion	11	626	1260	1480	
Emotional Pictures	12	0	0	0	
Pain: Warning	22	127	116	221	
Pain: Anticipation	22	74	55	182	

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#### What we'd like

- Don't threshold, model the signal!
  - Signal location?
    - Estimates and CI's on (x,y,z) location
  - Signal magnitude?
    - CI's on % change
  - Spatial extent?
    - Estimates and CI's on activation volume
    - Robust to choice of cluster definition
- ...but this requires an explicit spatial model



# Real-life inference: What we get

- Signal location
  - Local maximum no inference
  - Center-of-mass no inference
    - Sensitive to blob-defining-threshold
- Signal magnitude
  - Local maximum intensity P-values (& CI's)
- Spatial extent
  - Cluster volume P-value, no CI's
    - Sensitive to blob-defining-threshold

#### FWER vs. FDR

You **MUST** account for multiplicity (Otherwise have a fishing expedition)

- FWER
  - Very specific, not very sensitive

- FDR
  - Less specific, more sensitive
     (Sociological calibration still underway)

#### Conclusion

- There is a multiple testing problem and corrections must be applied on p-values, possibly for the volume of interest only (see SVC).
- Inference is made about topological features
   (peak height, spatial extent, number of clusters).
   Use results from the Random Field Theory.
   Or permutation tests.
- **Control of FWER** (probability of a false positive anywhere in the image) for a space of any dimension and shape.

#### References

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Flandin G and Friston KJ. Analysis of family-wise error rates in statistical parametric mapping using random field theory. Human Brain Mapping, 2017.

• And now a little demo!