

Introduction à la statistique médicale

Statistical Parametric Mapping short course

Course 4: Experimental Design

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Subtraction Logic

Cognitive subtraction originated with reaction time experiments (F. C. Donders, a Dutch physiologist).

Measure the time for a process to occur by comparing two reaction times, one which has the same components as the other + the process of interest.

Example:

T1: Hit a button when you see a light

T2: Hit a button when the light is green but not red

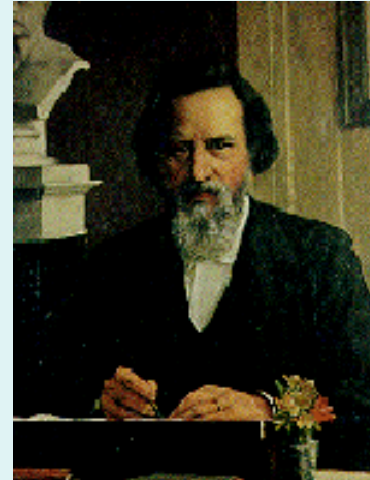
T3: Hit the left button when the light is green and the right button when the light is red

$T2 - T1 =$ time to make discrimination between light color

$T3 - T2 =$ time to make a decision

Assumption of pure insertion: You can insert a component process into a task without disrupting the other components.

Widely criticized (we'll come back to this when we talk about parametric studies)



Franciscus Cornelis
Donders (1818-1889)

Activation and baseline condition

Aim:

To reveal brain activation related to a cognitive or sensori-motor process of interest (PI)

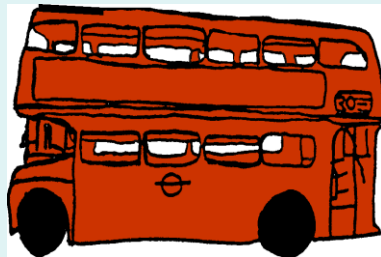
Cognitive Subtraction:

Contrast Activation task (engages PI) to a Baseline task (no PI).
Difference = Brain regions associated with PI.

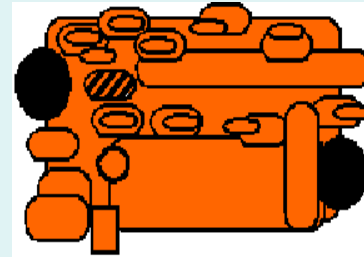
Example:

PI = Object recognition

Activation task: with PI



Baseline task: no PI

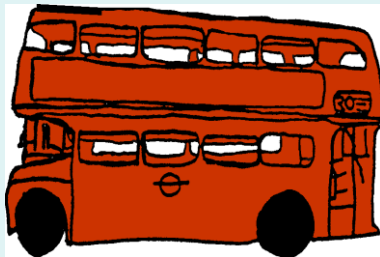


Difference = Brain regions associated with Object Recognition

Cognitive subtraction: stimulus or task change?

Stimulus Change

Activation condition

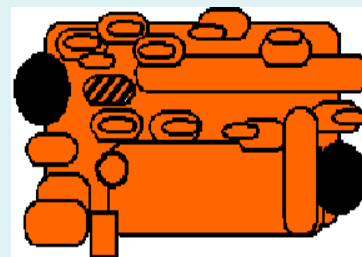


“View picture”

Task:
(constant)

—

Baseline condition



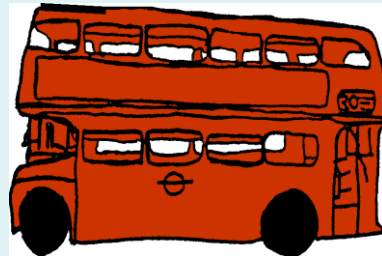
“View picture”

=

**Object
Recognition**

Stimulus (constant)

Activation condition

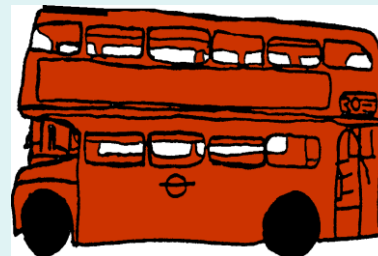


“Name Object”

Task: Change:

—

Baseline condition



“Say: “Yes””

=

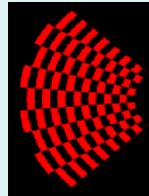
**Name
Retrieval**

Cognitive Subtraction: Baseline problems

- „Distant“ stimuli



-



→ Several components differ!

- „Related“ stimuli



-



→ *Process* implicit in control task ?

„Queen!“

„Aunt Jenny?“

- Same stimuli, different task



-



→ Interaction of process and task ?

Name Person!

Name Gender!

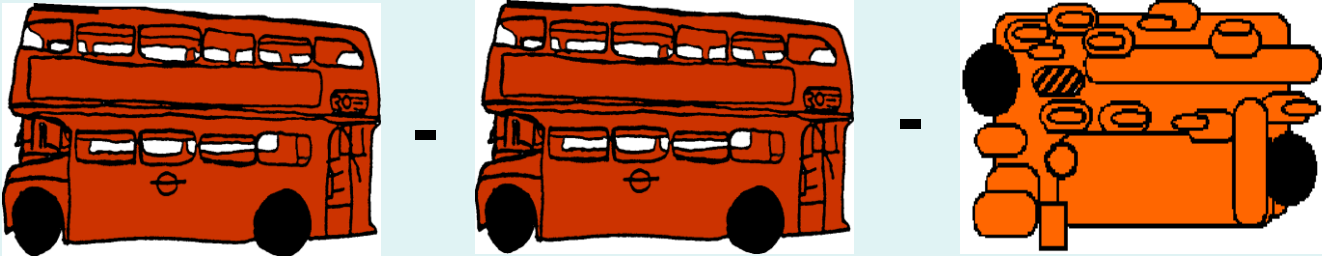
Cognitive subtraction: serial subtractions

Baseline condition for one contrast acts as activation condition for another contrast

Example:

Stimulus:

Condition A. Condition B. Condition C.



Task: **Name Object** **Say: "Yes"** **Say: "Yes"**

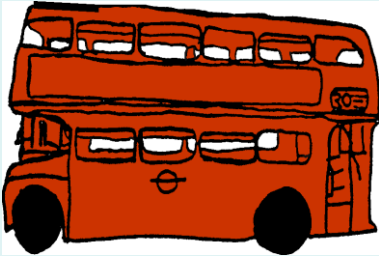
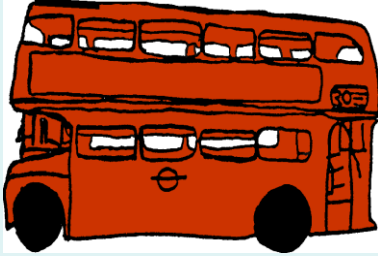
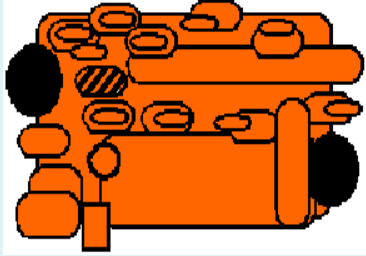
A-B = Name Retrieval

B-C = Object Recognition

Very limited...

Problem with serial subtractions

Stimulus:

	Condition A	Condition B	Condition C
			
Task:	Say: Name of Object	Say: "Yes"	Say: "Yes"

Assumptions:

- A - B = only changes processing associated with Name Retrieval
- B - C = only changes processing associated with Object Recognition

BUT

1. There may be *implicit* naming in condition B. In which case: naming component is removed from A-B and introduced into B-C.
 2. Name Retrieval may increase the demands on object recognition
- i.e A - B : May reveal Object recognition NOT Name retrieval.
B - C : May reveal Object Recognition AND Name Retrieval

Factorial design: main effects & interaction

		Task (1/2)	
		Viewing	Naming
Stimuli (A/B)	Colours	A1	A2
	Objects	B1	B2

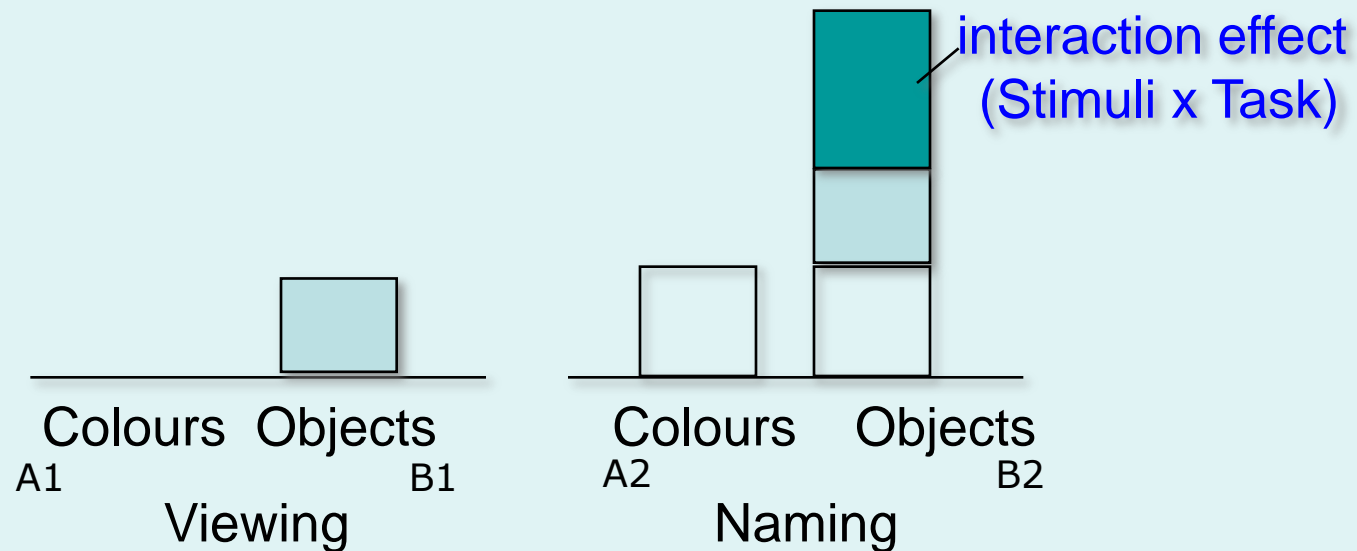
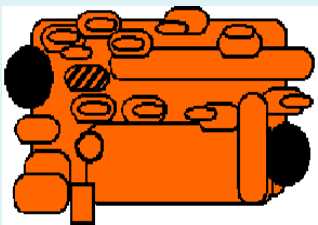
Main effect of task:
 $(A1 + B1) - (A2 + B2)$

Main effect of stimuli:
 $(A1 + A2) - (B1 + B2)$

Object



Colour



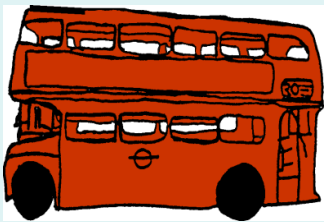
Factorial design: main effects & interaction

		Task (1/2)	
		Viewing	Naming
Stimuli (A/B)	Colours	A1	A2
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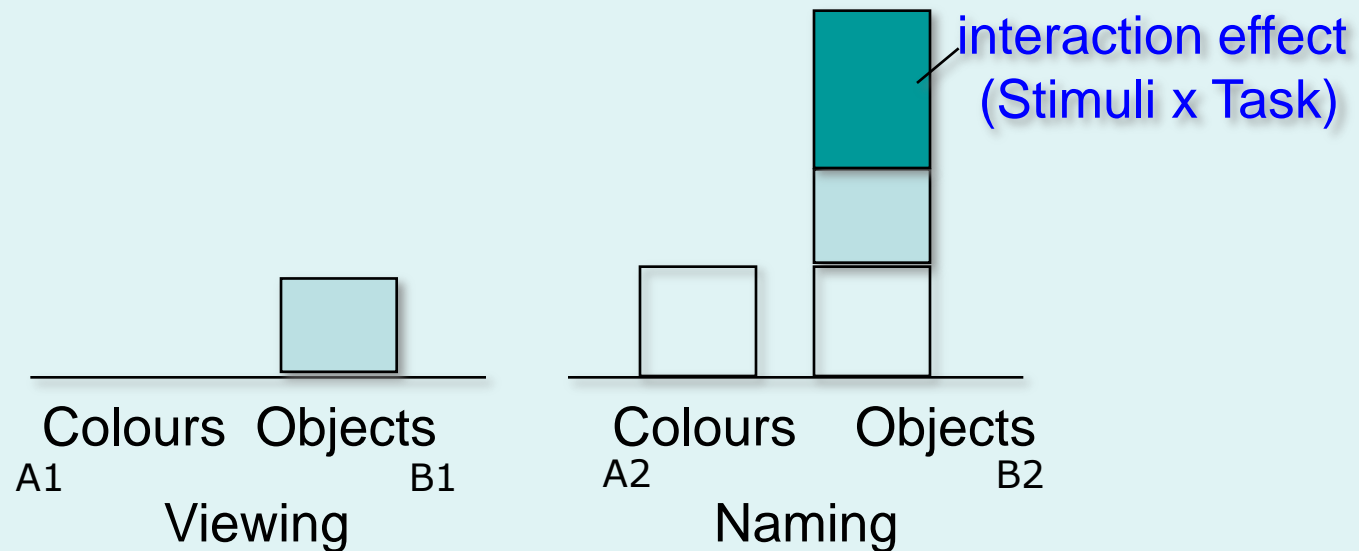
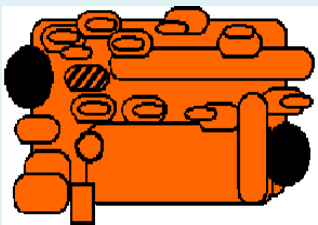
B2 – A2 = Object Recognition
during naming

B1 – A1 = Object Recognition
during viewing

Object



Colour



Factorial design: main effects & interaction

Task (1/2)

		Viewing	Naming
Stimuli (A/B)	Colours	A1	A2
	Objects	B1	B2

Interaction of task and stimuli:
Can show a failure of pure insertion

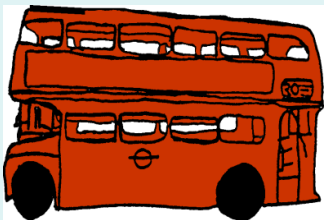
$$(B1 - A1) - (B2 - A2)$$

The effect of Naming on Object recognition

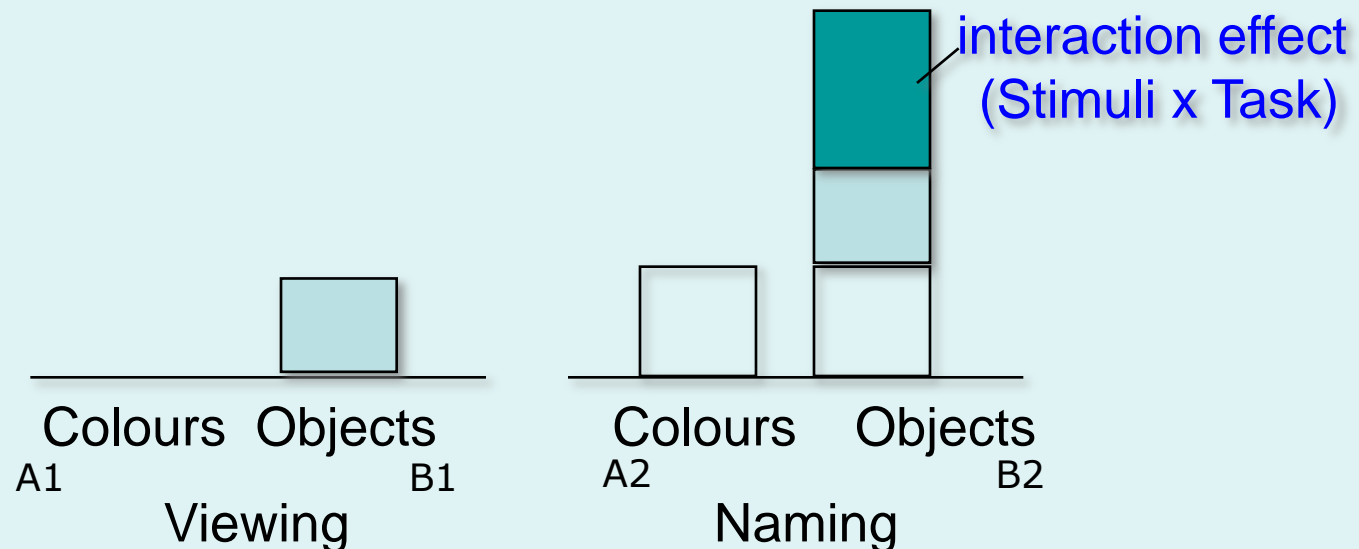
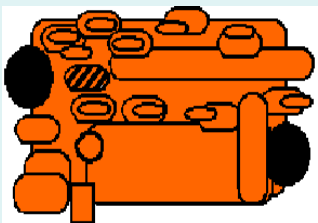
$$(A2 - A1) - (B2 - B1)$$

The effect of object recognition on Naming

Object



Colour



Parametric Designs: General Approach

- Parametric designs approach the baseline problem by:
 - Varying the stimulus-parameter of interest on a continuum, in multiple ($n > 2$) steps...
 - ... and relating signal to this parameter
- Possible tests for such relations are manifold:
 - Linear
 - Nonlinear: Quadratic/cubic/etc.
 - „Data-driven“ (e.g., neurometric functions)

Parametric design

- No need to find baseline that controls for all but the process of interest
- Segregates areas showing differential effects (linear and nonlinear effects)

But:

- Common effects can not be revealed without a baseline.
- Limited to continuous variables (e.g. duration, frequency, word length, R.T.s etc)

Parametric design: Model-based regressors

“Signals derived from a computational model for a specific cognitive process are correlated against BOLD from participants performing a relevant task, to determine brain regions showing a response profile consistent with that model.”

The model describes a transformation between a set of stimuli inputs and a set of behavioural responses.

See e.g. O’Doherty et al., (2007) for a review.

Model-based regressors: Example

Question

Is the hippocampus sensitive to the probabilistic context established by event streams? Rather than simply responding to the event itself.

The same question can be formulated in a quantitative way by using the information theoretic quantities ‘entropy’ and ‘surprise’.

- ‘surprise’ is unique to a particular event and measures its improbability.

$$I(x_i) = -\ln p(x_i);$$

- ‘entropy’ is the measure of the expected, or average, surprise over all events, reflecting the probability of an outcome before it occurs.

$$H(X) = \sum_i -p(x_i) \ln p(x_i) = \langle I(x_i) \rangle$$

x_i is the occurrence of an event. $H(X)$ quantifies the expected info of events sampled from X .

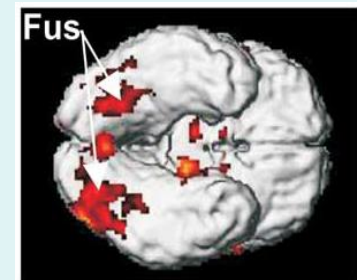
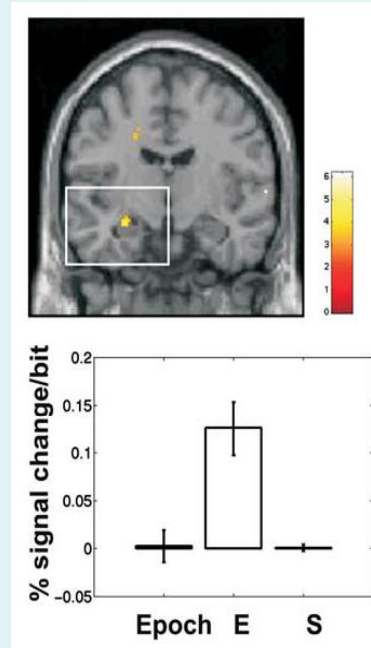
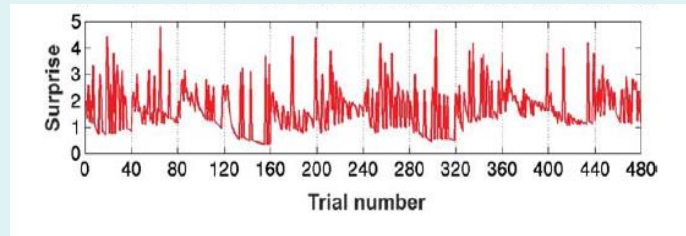
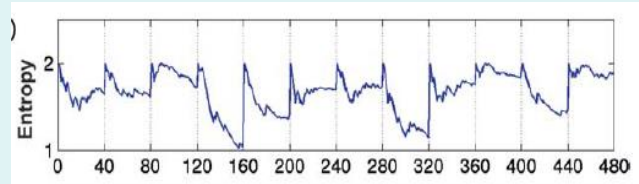
Thus, hippocampus would be expected to process ‘entropy’ and not ‘surprise’.

Model-based regressors: Example



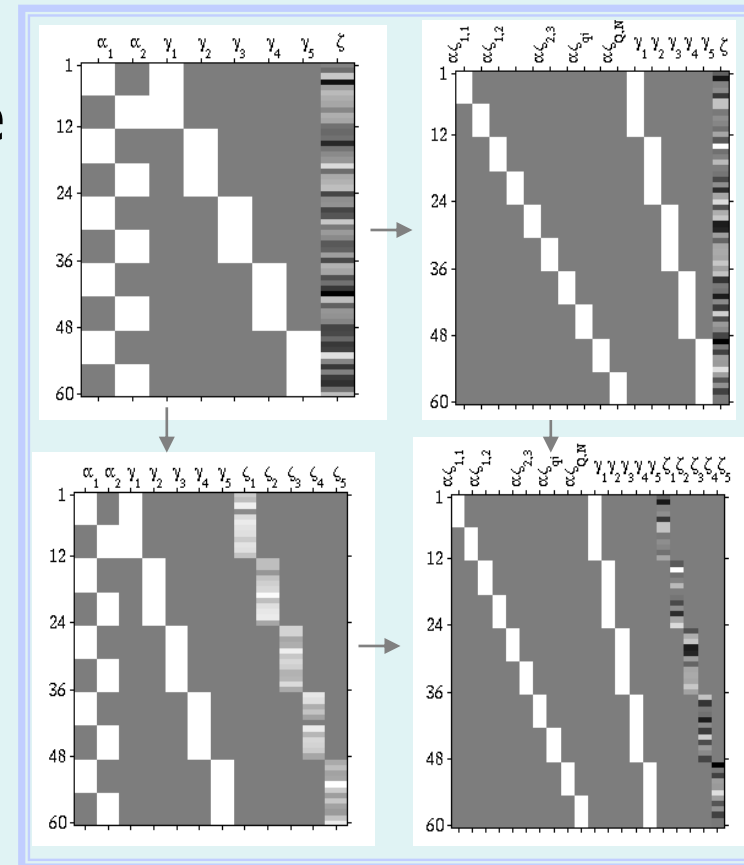
Participants responded to the sampled item by pressing a key to indicate the position of that item in the row of alternative coloured shapes.

The participants will learn the probability with which a cue appears.



Model selection

- Model must fit *i.e. model assumptions met*
 - at **every** voxel
- Omitting relevant effects
 - effects contribute to variance
 - ⇒ residuals not *iid*. Normal
 - ☹ model not valid
 - outcomes?
 - variance ↑ (*usually, but can* ↓)
 - increased residual *d.f.*
 - invalid inference
- Including irrelevant effects
 - ☹ “waste” degrees of freedom
 - ☹ conservative tests
 - but safest!



Conclusions...

General Linear Model

- (simple) standard statistical technique
 - temporal autocorrelation – *a Generalised Linear Model*
- single general framework for many statistical analyses
 - flexible modelling \Leftarrow basis functions
- design matrix visually characterizes model
 - fit data with combinations of columns of design matrix
- statistical inference: *contrasts*...
 - *t*-tests: planned comparisons of the parameters
 - *F*-tests: general linear hypotheses, model comparison

Three Stages of an Experiment

1. Sledgehammer Approach

- brute force experiment : powerful stimulus & don't try to control for everything
- look at what was done before or by others
- run a couple of subjects -- see if it looks promising
- if it doesn't look great, tweak the stimulus or task
- try to be a subject yourself so you can notice any problems with stimuli or subject strategies

Three Stages of an Experiment

1. Sledgehammer Approach

2. Real Experiment

- at some point, you have to stop changing things and collect enough subjects run with the same conditions to publish it
- how many subjects do you need
 - some psychophysical studies test two or three subjects, many studies test 6-10 subjects, random effects analysis requires at least 15 subjects,...
 - some subjects WILL be rejected, so acquire more than the minimum !
- can run all subjects in one or two days
 - pro: minimize setup and variability
 - con: “bad magnet day” means a lot of wasted time
 - make sure all the data are treated the “same way”. (script)

Three Stages of an Experiment

1. Sledgehammer Approach

2. Real Experiment

3. “Whipped Cream” experiment

- after the real experiment works, then think about a “whipped cream” version
- going straight to whipped cream is a huge endeavor, especially if you’re new to imaging
- and it gives you a second paper !

